

Influence of H₂ formation on PDR model results

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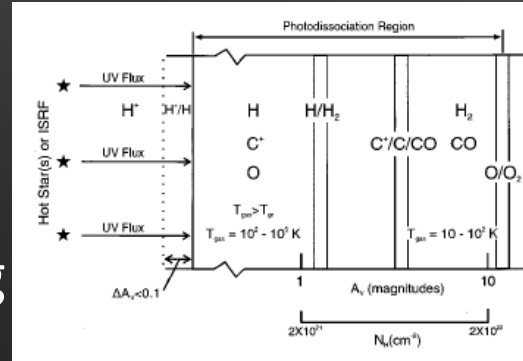
Universität zu Köln, Germany

Outline

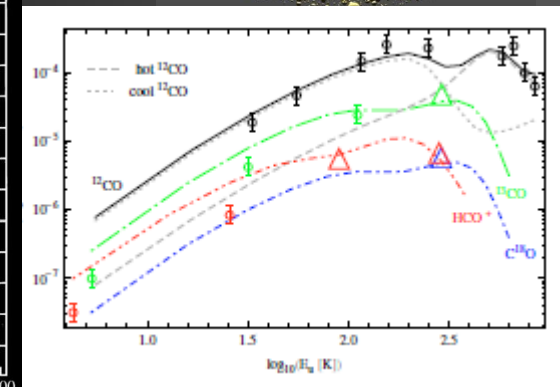
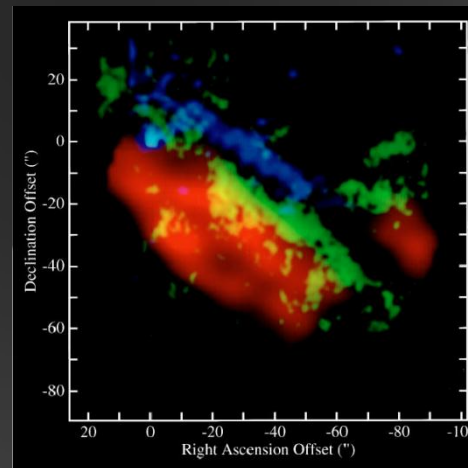
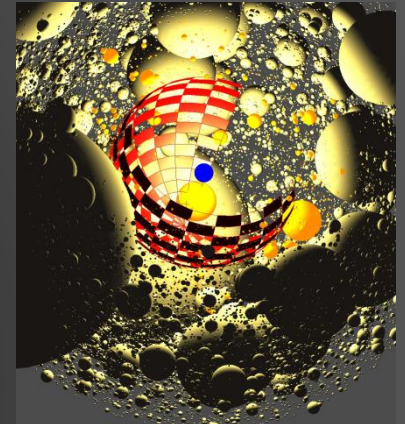
- H₂ formation on grain surfaces
 - chemisorption vs. physisorption
 - H₂ formation efficiencies on different dust sorts
 - chemical H₂ heating & cooling
 - effects on clump structure

Introduction

Numerical PDR models of proved to be a valuable tools in analyzing and understanding the local conditions in massive star forming regions.



Hollenbach & Tielens, 1999, R.o.m.P., 71

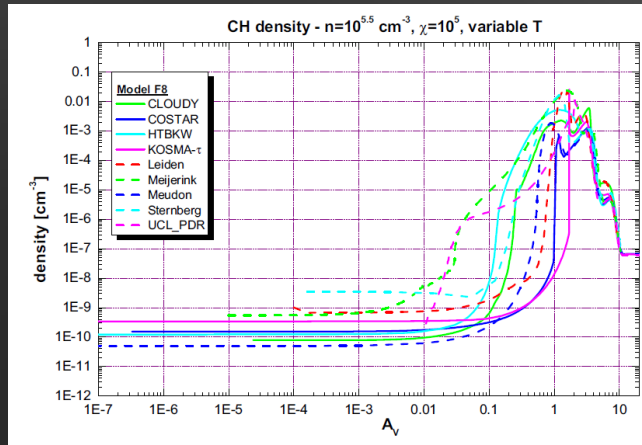


Ossenkopf et al, 2010, A&A 518, L79v

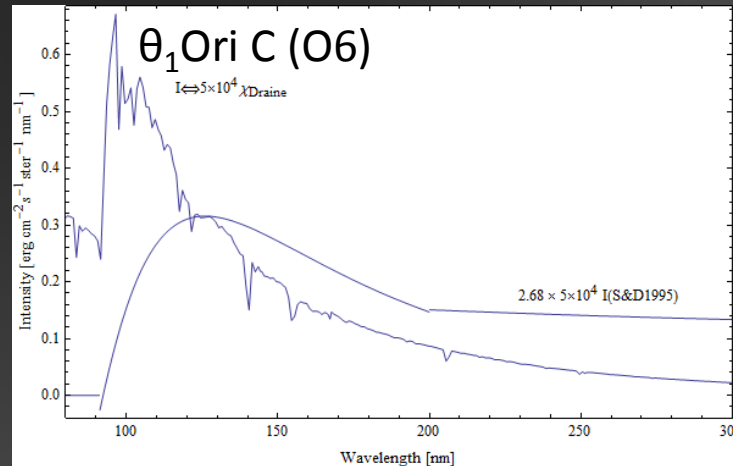
Introduction

Yet, here be dragons...

- complex physics / chemistry
- complex/unknown local conditions



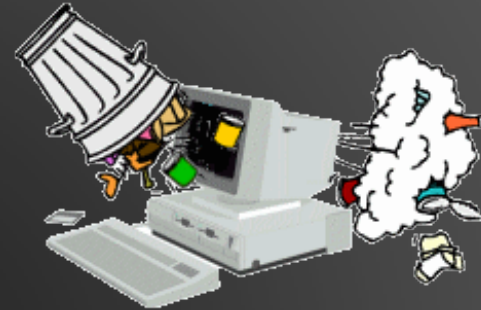
Röllig et al. 2007, A&A, 467



Introduction

and unfortunately, deficient
input data

- missing experimental data
- inter/extrapolation



H₂ formation on grain surfaces

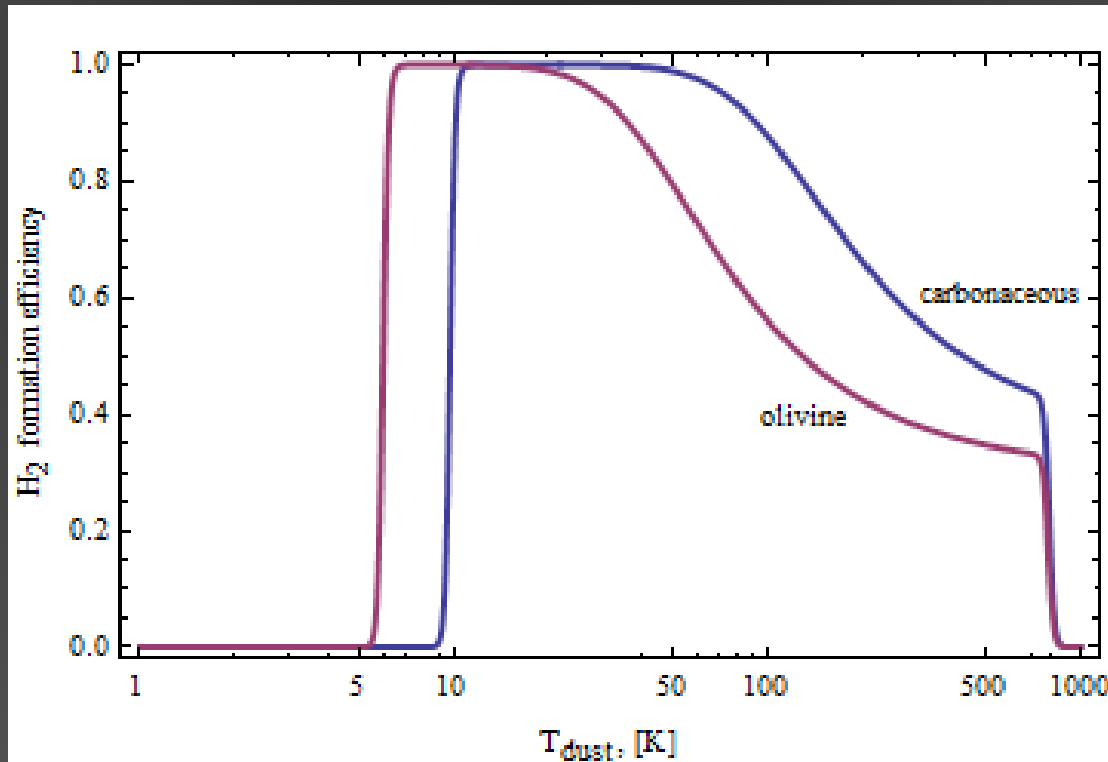
H₂ formation on grain surfaces

- H atoms hitting grain surfaces can stick weakly (physisorption) or strongly (chemisorption) bound.
- $T_d > 100$ K desorption overcomes binding and H₂ formation efficiency $\rightarrow 0$
- Chemisorbed H atoms can effectively form H₂ up to $T_d > 500$ K
- we implemented the formalism presented by Cazaux & Tielens (2002,2004) in the KOSMA- τ chemistry.

H₂ formation efficiency

$$\epsilon_{H_2} = \left(\frac{\mu F}{2\beta_{H_2}} + 1 + \frac{\beta_{HP}}{\alpha_{pc}} \right)^{-1}$$

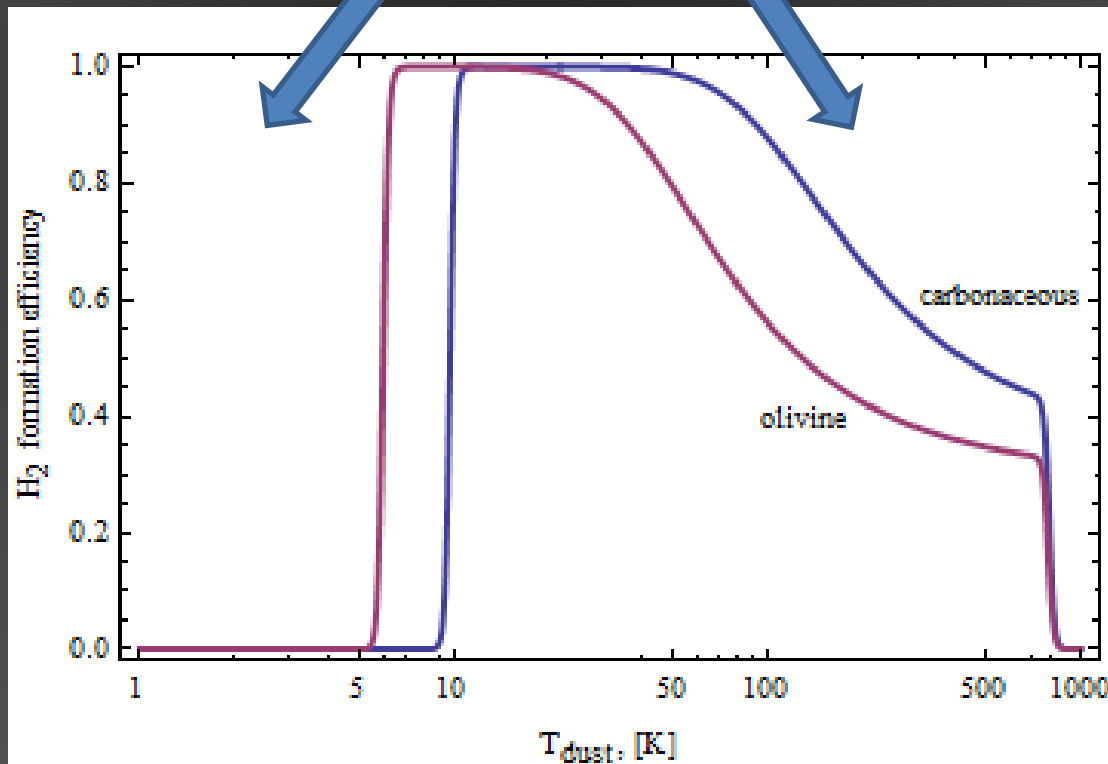
Cazaux & Tielens 2004, ApJ 604



H₂ formation efficiency

$$\epsilon_{H_2} = \left(\frac{\mu F}{2\beta_{H_2}} + 1 + \frac{\beta_{HP}}{\alpha_{pc}} \right)^{-1}$$

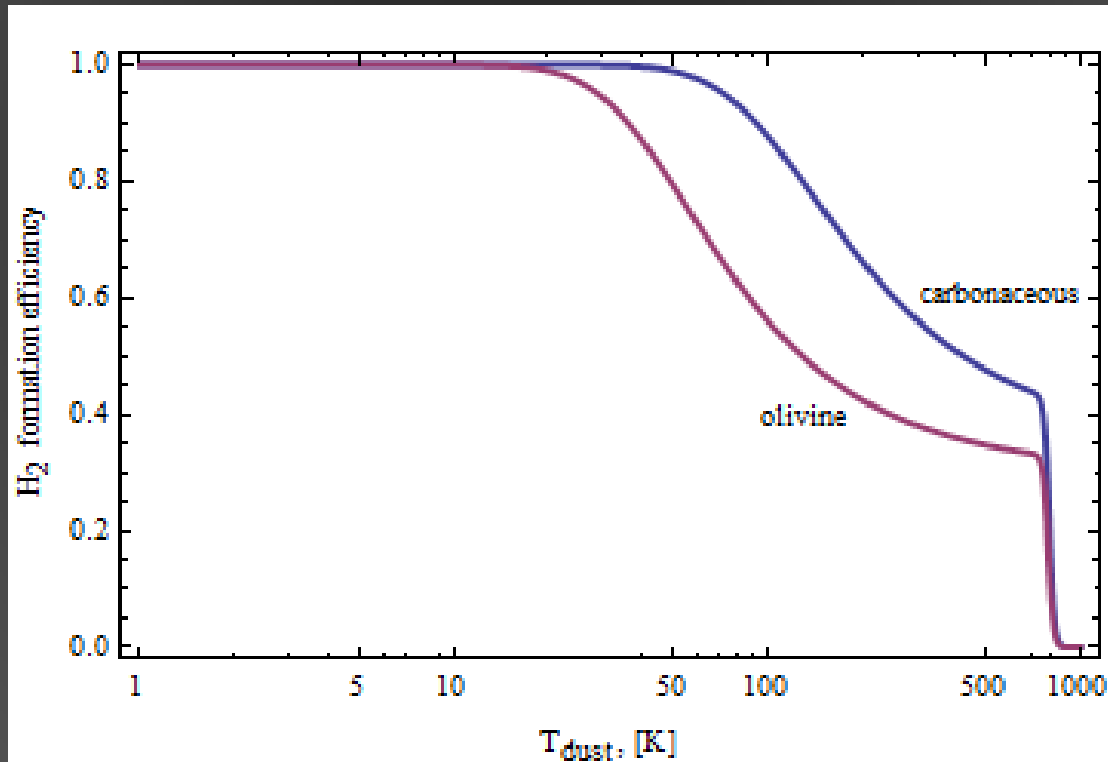
Cazaux & Tielens 2004, ApJ 604



H₂ formation efficiency

$$\epsilon_{H_2} = \left(\frac{\mu F}{2\beta_{H_2}} + 1 + \frac{\beta_{HP}}{\alpha_{pc}} \right)^{-1}$$

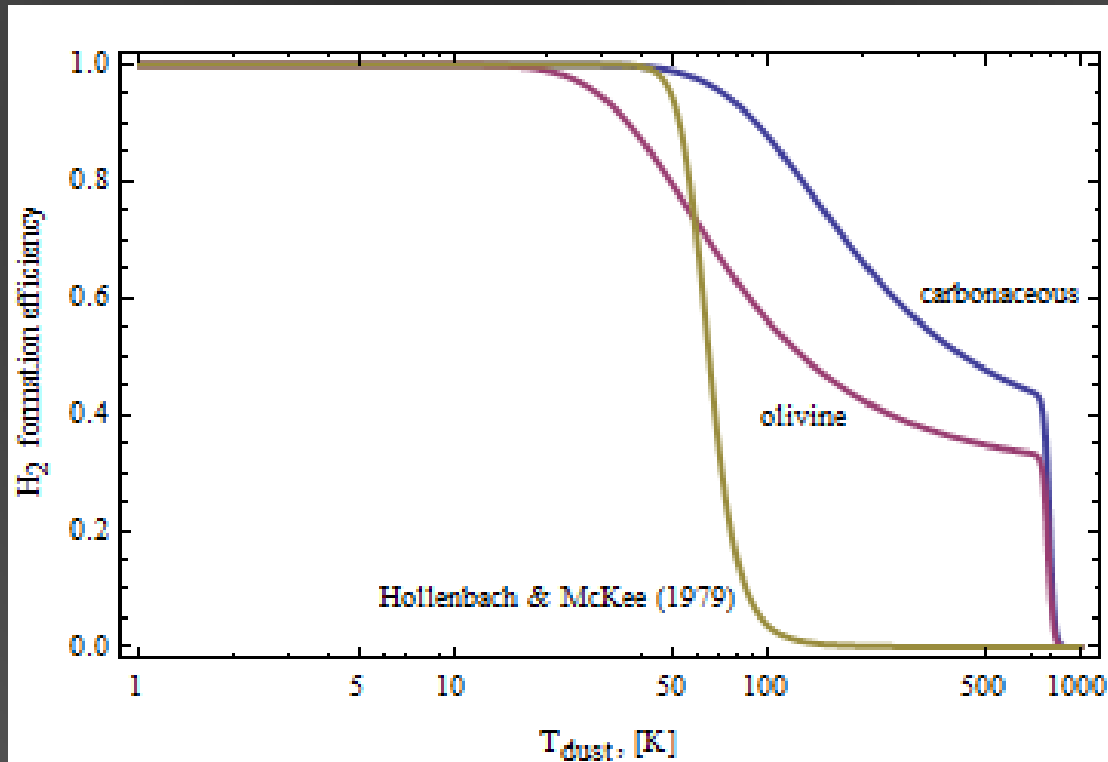
Cazaux & Tielens 2004, ApJ 604



H₂ formation efficiency

$$\epsilon_{H_2} = \left(\frac{\mu F}{2\beta_{H_2}} + 1 + \frac{\beta_{HP}}{\alpha_{pc}} \right)^{-1}$$

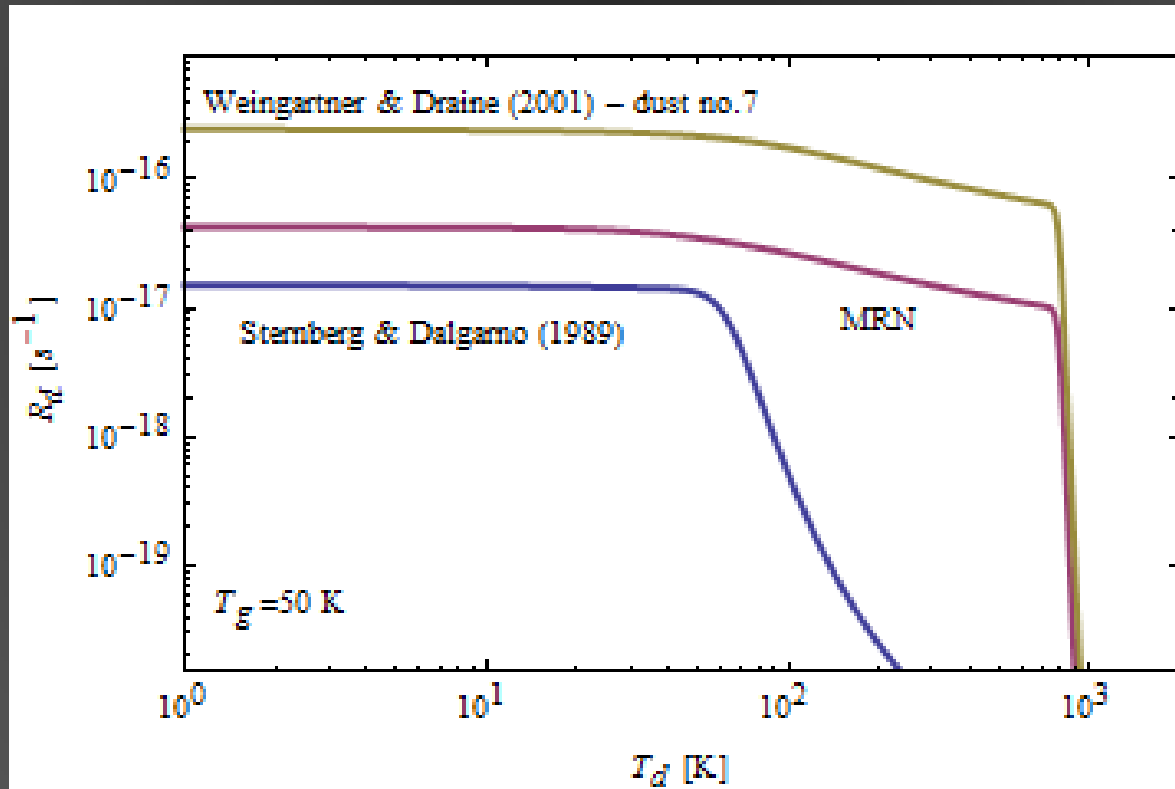
Cazaux & Tielens 2004, ApJ 604



H₂ formation rate

total formation rate
depends on total dust
surface

$$R_d = \frac{1}{2} n(H) v_H n_d \sigma_d \epsilon_{\text{H}_2} S_H$$



H₂ formation rate

TABLE 1
GRAIN-SIZE DISTRIBUTION PARAMETER VALUES^a

R_V^b	$10^5 b_c^c$	Case	α_g	β_g	$a_{v,g}$ (μm)	$a_{r,g}$ (μm)	C_g	α_x	β_x	$a_{v,x}$ (μm)	C_x	\tilde{V}_g^d	\tilde{V}_x^d	χ_1^{2e}	χ_2^{2f}	χ^{2g}
3.1	0.0	A	-2.25	-0.0648	0.00745	0.606	9.94×10^{-11}	-1.48	-9.34	0.172	1.02×10^{-12}	1.146	1.244	0.047	0.111	0.118
3.1	1.0	A	-2.17	-0.0382	0.00373	0.586	3.79×10^{-10}	-1.46	-10.3	0.174	1.09×10^{-12}	1.137	1.251	0.047	0.116	0.118
3.1	2.0	A	-2.04	-0.111	0.00828	0.543	5.57×10^{-11}	-1.43	-11.7	0.173	1.27×10^{-12}	1.130	1.254	0.048	0.124	0.118
3.1	3.0	A	-1.91	-0.125	0.00837	0.499	4.15×10^{-11}	-1.41	-11.5	0.171	1.33×10^{-12}	1.119	1.260	0.049	0.139	0.119
3.1	4.0	A	-1.84	-0.132	0.00898	0.489	2.90×10^{-11}	-2.10	-0.114	0.169	1.26×10^{-13}	1.113	1.290	0.048	0.135	0.126
3.1	5.0	A	-1.72	-0.322	0.0254	0.438	3.20×10^{-12}	-2.10	-0.0407	0.166	1.27×10^{-13}	1.098	1.304	0.051	0.154	0.131
3.1	6.0	A	-1.54	-0.165	0.0107	0.428	9.99×10^{-12}	-2.21	0.300	0.164	1.00×10^{-13}	1.092	1.322	0.052	0.161	0.136
4.0	0.0	A	-2.26	-0.199	0.0241	0.861	5.47×10^{-12}	-2.03	0.668	0.189	5.20×10^{-14}	1.000	1.100	0.036	0.100	0.048
4.0	1.0	A	-2.16	-0.0862	0.00867	0.803	4.58×10^{-11}	-2.05	0.832	0.188	4.81×10^{-14}	0.992	1.103	0.035	0.104	0.048
4.0	2.0	A	-2.01	-0.0973	0.00811	0.696	3.96×10^{-11}	-2.06	0.995	0.185	4.70×10^{-14}	0.974	1.112	0.035	0.113	0.050
4.0	3.0	A	-1.83	-0.175	0.0117	0.604	1.42×10^{-11}	-2.08	1.29	0.184	4.26×10^{-14}	0.957	1.121	0.036	0.130	0.053
4.0	4.0	A	-1.64	-0.247	0.0152	0.536	5.83×10^{-12}	-2.09	1.58	0.183	3.94×10^{-14}	0.933	1.145	0.037	0.148	0.060
5.5	0.0	A	-2.35	-0.668	0.148	1.96	4.82×10^{-14}	-1.57	1.10	0.198	4.24×10^{-14}	0.889	1.076	0.034	0.110	0.043
5.5	1.0	A	-2.12	-0.670	0.0686	1.35	3.65×10^{-13}	-1.57	1.25	0.197	4.00×10^{-14}	0.848	1.078	0.034	0.115	0.043
5.5	2.0	A	-1.94	-0.853	0.0786	0.921	2.57×10^{-13}	-1.55	1.33	0.195	4.05×10^{-14}	0.804	1.095	0.032	0.118	0.044
5.5	3.0	A	-1.61	-0.722	0.0418	0.720	7.58×10^{-13}	-1.59	2.12	0.193	3.20×10^{-14}	0.768	1.118	0.033	0.128	0.049
4.0	0.0	B	-2.62	-0.0144	0.0187	5.74	6.46×10^{-12}	-2.01	0.894	0.198	4.95×10^{-14}	0.011	0.042	...
4.0	1.0	B	-2.52	-0.0541	0.0366	6.65	1.08×10^{-12}	-2.11	1.58	0.197	3.69×10^{-14}	0.011	0.043	...
4.0	2.0	B	-2.36	-0.0957	0.0305	6.44	1.62×10^{-12}	-2.05	1.19	0.197	4.37×10^{-14}	0.011	0.042	...
4.0	3.0	B	-2.09	-0.193	0.0199	4.60	4.21×10^{-12}	-2.10	1.64	0.198	3.63×10^{-14}	0.011	0.044	...
4.0	4.0	B	-1.96	-0.813	0.0693	3.48	2.95×10^{-13}	-2.11	2.10	0.198	3.13×10^{-14}	0.017	0.056	...
5.5	0.0	B	-2.80	0.0356	0.0203	3.43	2.74×10^{-12}	-1.09	-0.370	0.218	1.17×10^{-13}	0.017	0.092	...
5.5	1.0	B	-2.67	0.0129	0.0134	3.44	7.25×10^{-12}	-1.14	-0.195	0.216	1.05×10^{-13}	0.017	0.088	...
5.5	2.0	B	-2.45	-0.00132	0.0275	5.14	8.79×10^{-13}	-1.08	-0.336	0.216	1.17×10^{-13}	0.017	0.085	...
5.5	3.0	B	-1.90	-0.0517	0.0120	7.28	2.86×10^{-12}	-1.13	-0.109	0.211	1.04×10^{-13}	0.017	0.082	...

^a See eqs. (4) and (5). In all cases, we take $a_{v,x} = 0.1 \mu\text{m}$.

^b $R_V = A(V)/E_{B-V}$, ratio of visual extinction to reddening.

^c C abundance in double log-normal very small grain population (see eqs. [2] and [3]).

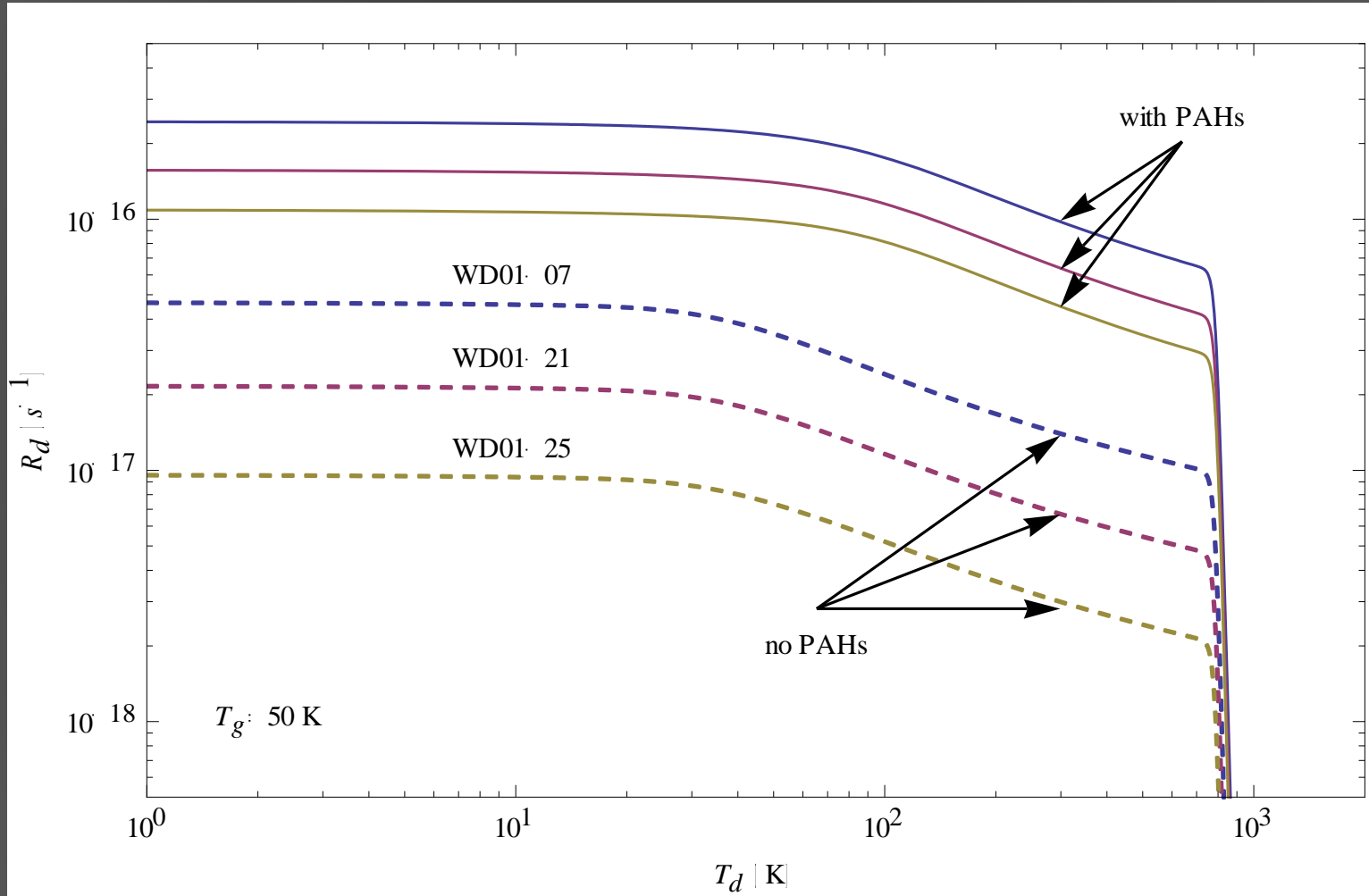
^d Total grain volumes in the carbonaceous and silicate populations, normalized to their abundance/depletion-limited values (2.07×10^{-27} and $2.98 \times 10^{-27} \text{ cm}^3 \text{ H}^{-1}$, respectively).

^e $\chi_1^2 = \sum_i (\ln A_{obs} - \ln A_{mod})^2 / \sigma_i^2$, for 100 points equally spaced in $\ln \lambda$.

^f $\chi_2^2 = \sum_j (\ln A_{obs} - \ln A_{mod})^2$.

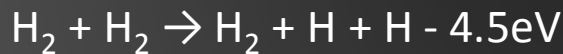
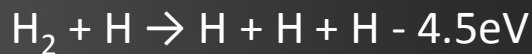
^g $\chi^2 = \chi_1^2 + 0.4(\tilde{V}_g - 1)^{1.5} + 0.4(\tilde{V}_x - 1)^{1.5}$.

H₂ formation rate



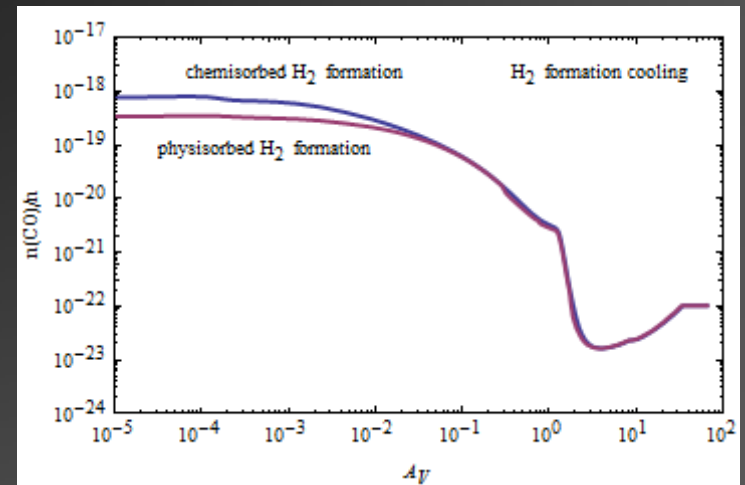
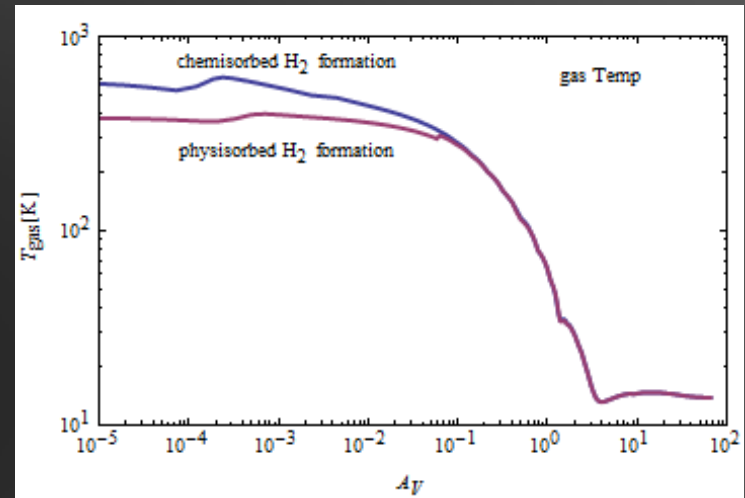
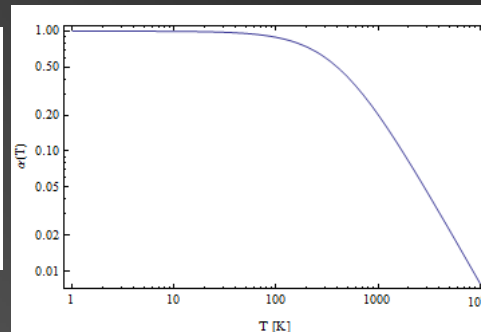
H₂ heating/cooling

- H₂ binding energy 4.5 eV
→ H₂ formation heating
- kinetic H₂ dissociation cooling
(Lepp & Shull, 1983, ApJ 270, 578)

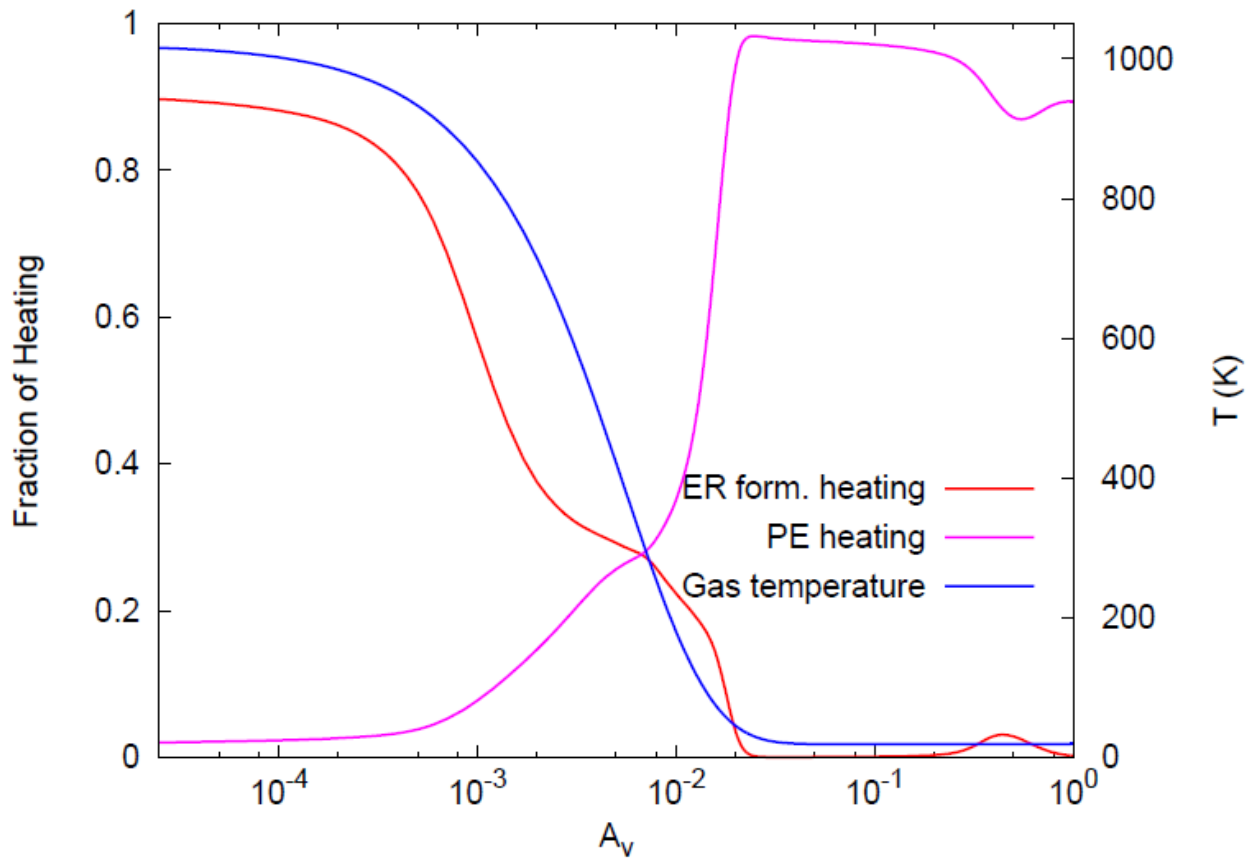


Alternatively: sticking coeff.

$$\alpha(T) = \frac{1}{1 + \left(\frac{T}{T_2}\right)^\beta}.$$



H₂ heating/cooling



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H₂ heating/cooling

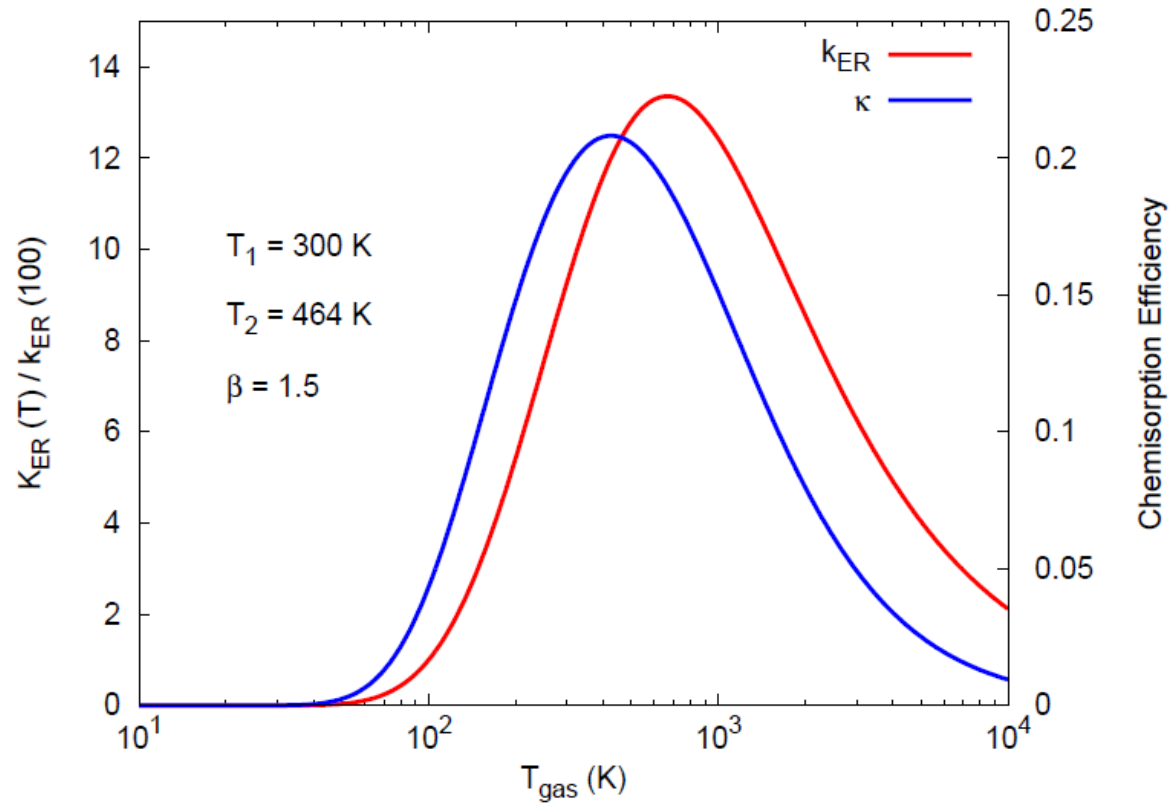


Figure C.1. Left axis: Variation of k_{ER} with gas temperature T (relative to the one at 100K). Right axis: chemisorption efficiency κ (see text).

H₂ heating/cooling

Table 4. Model results for $P = 10^5 \text{ cm}^{-3} \text{ K}$ and three different radiation field enhancements. Models A, B, and C are identical as previously and defined in the text. Here l is the total width of the cloud expressed in pc, corresponding to a total visual magnitude of 10, $N(X)$ stands for the resulting total column density of species X, and exponent “obs” means values at the edge of the cloud on the observer side. Numbers in parenthesis give the powers of ten.

	10^2			10^3			10^4		
χ^{obs}									
T_g^{obs} (min) (K)	16.7			26.2			41		
T_g^{obs} (max) (K)	27.7			44.1			70		
Model	A	B	C	A	B	C	A	B	C
l (pc)	1.0	1.0	1.0	2.1	2.2	2.1	3.15	3.6	3.4
n_H^{obs} (cm^{-3})	364	374	353	398	414	378	566	584	566
T^{obs} (K)	250	243	258	228	219	241	161	156	160
$R_{H_2}^{obs}$ ($\text{cm}^3 \text{ s}^{-1}$)	3(-17)	1.2(-18)	1.1(-16)	3(-17)	1.9(-26)	9.8(-17)	3.0(-17)	5.2(-31)	5.3(-17)
A_V (H = H ₂)	0.41	0.55	0.28	0.94	1.5	0.78	1.54	...	3.6
$n_{\text{H(H=H}_2\text{)}} (\text{cm}^{-3})$	930	1.3(3)	747	750	1.58(3)	676	706	...	3.6(3)
$T_{\text{(H=H}_2\text{)}} (\text{K})$	142	97	172	172	83	193	182	...	35
$N(\text{H}) (\text{cm}^{-2})$	6.7(20)	9.8(20)	5.0(20)	1.7(21)	2.8(21)	1.4(21)	2.8(21)	1.8(22)	1.3(22)
$N(\text{H}_2) (\text{cm}^{-2})$	9.0(21)	8.9(21)	9.1(21)	8.5(21)	8.0(21)	8.6(21)	8.0(21)	5.6(20)	2.7(21)

A: R=const, B: only LH, C=LH+ER

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H₂ heating/cooling

Table 9. Emissivities of H₂ transitions in erg cm⁻² s⁻¹ sr⁻¹. Number in parenthesis refer to powers of ten.
*R*₁ : 1 – 0S(1)/2 – 1S(1), *R*₂ : 1 – 0S(1)/1 – 0S(7), *R*₃ : 1 – 0S(1)/6 – 4O(3),

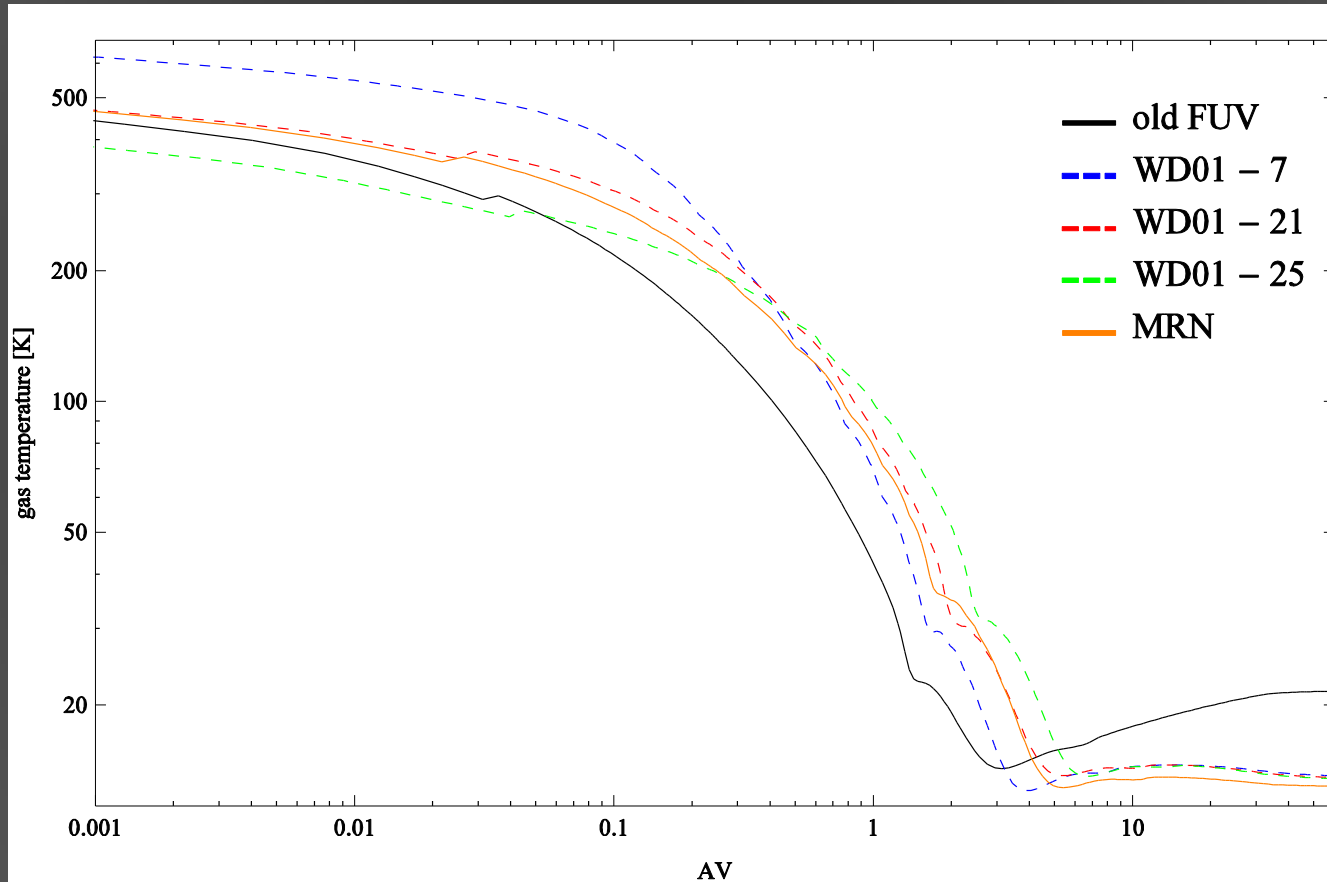
<i>p</i> (cm ⁻³ K)	<i>χ</i> _{obs} Model	10 ²			10 ³			10 ⁴		
		A	B	C	A	B	C	A	B	C
10 ⁵	0-0 S(0)	2.1(-6)	4.4(-7)	3.8(-6)	7.0(-6)	2.3(-7)	1.1(-5)	1.3(-5)	2.1(-10)	1.7(-5)
	0-0 S(1)	1.2(-6)	1.2(-7)	3.5(-6)	5.8(-6)	4.0(-8)	1.2(-5)	1.5(-5)	6.0(-10)	2.4(-5)
	0-0 S(2)	1.5(-7)	7.1(-8)	2.6(-7)	2.8(-7)	3.2(-8)	6.4(-7)	5.1(-7)	1.0(-9)	9.8(-7)
	0-0 S(3)	2.1(-7)	9.5(-8)	3.4(-7)	3.2(-7)	4.0(-8)	6.7(-7)	4.0(-7)	4.5(-10)	8.0(-7)
	1-0 S(1)	4.0(-7)	1.6(-7)	6.3(-7)	8.1(-7)	5.9(-8)	1.6(-6)	1.1(-6)	1.2(-9)	2.1(-6)
	<i>R</i> ₁	2.0	2.0	2.0	1.9	2.0	1.9	1.9	1.9	1.9
	<i>R</i> ₂	7.5	7.1	5.4	7.7	8.3	4.9	7.4	91	4.8
	<i>R</i> ₃	3.6	3.7	3.5	4.0	3.7	3.9	4.0	4.2	4.0
10 ⁶	0-0 S(0)	1.9(-6)	3.3(-7)	2.3(-6)	1.2(-5)	3.2(-7)	1.8(-5)	2.2(-5)	1.3(-9)	2.9(-5)
	0-0 S(1)	6.2(-7)	6.4(-7)	9.7(-7)	1.4(-5)	3.2(-8)	4.4(-5)	4.7(-5)	1.3(-9)	1.1(-4)
	0-0 S(2)	3.8(-7)	1.9(-7)	4.5(-7)	3.1(-6)	9.4(-8)	1.3(-5)	1.1(-5)	4.8(-9)	2.8(-5)
	0-0 S(3)	4.7(-7)	2.5(-7)	5.3(-7)	1.4(-6)	1.1(-7)	3.4(-6)	2.1(-6)	3.0(-9)	5.6(-6)
	1-0 S(1)	6.7(-7)	3.2(-7)	7.4(-7)	2.8(-6)	1.4(-7)	5.6(-6)	4.5(-6)	6.6(-9)	9.2(-6)
	<i>R</i> ₁	2.0	2.0	2.0	2.0	2.0	1.9	1.9	2.0	1.9
	<i>R</i> ₂	4.2	3.9	3.2	5.2	5.1	3.7	5.2	22	3.4
	<i>R</i> ₃	4.1	4.8	4.0	4.2	5.0	4.0	4.2	6.3	4.1
10 ⁷	0-0 S(0)	2.2(-7)	1.1(-7)	1.7(-7)	7.9(-6)	1.9(-7)	1.1(-5)	1.9(-5)	4.5(-9)	2.5(-5)
	0-0 S(1)	1.2(-8)	7.8(-9)	9.5(-9)	1.0(-5)	7.7(-9)	3.7(-5)	7.5(-5)	1.0(-9)	2.0(-4)
	0-0 S(2)	1.1(-7)	1.2(-7)	1.1(-7)	5.4(-6)	1.2(-7)	2.5(-5)	4.6(-5)	1.5(-8)	1.4(-4)
	0-0 S(3)	4.8(-7)	3.9(-7)	4.5(-7)	4.5(-6)	2.7(-7)	1.1(-5)	1.4(-5)	2.0(-8)	9.0(-5)
	1-0 S(1)	3.7(-7)	2.9(-7)	3.4(-7)	5.8(-6)	2.4(-7)	9.5(-6)	1.3(-5)	2.9(-8)	2.5(-5)
	<i>R</i> ₁	2.2	2.3	2.1	2.1	2.2	2.1	2.1	2.3	2.1
	<i>R</i> ₂	1.4	1.4	1.2	2.6	2.0	2.2	3.0	6.5	2.3
	<i>R</i> ₃	7.0	11	8.2	5.2	11	4.4	4.7	15	4.4

A: R=const, B: only LH, C=LH+ER

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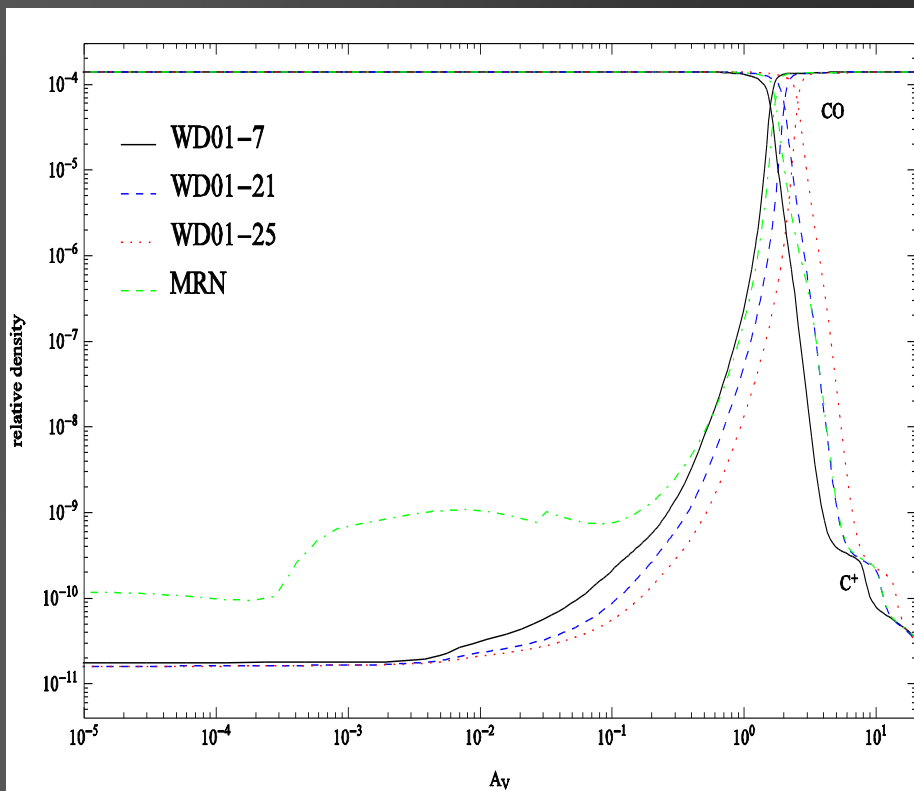
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Dust influence

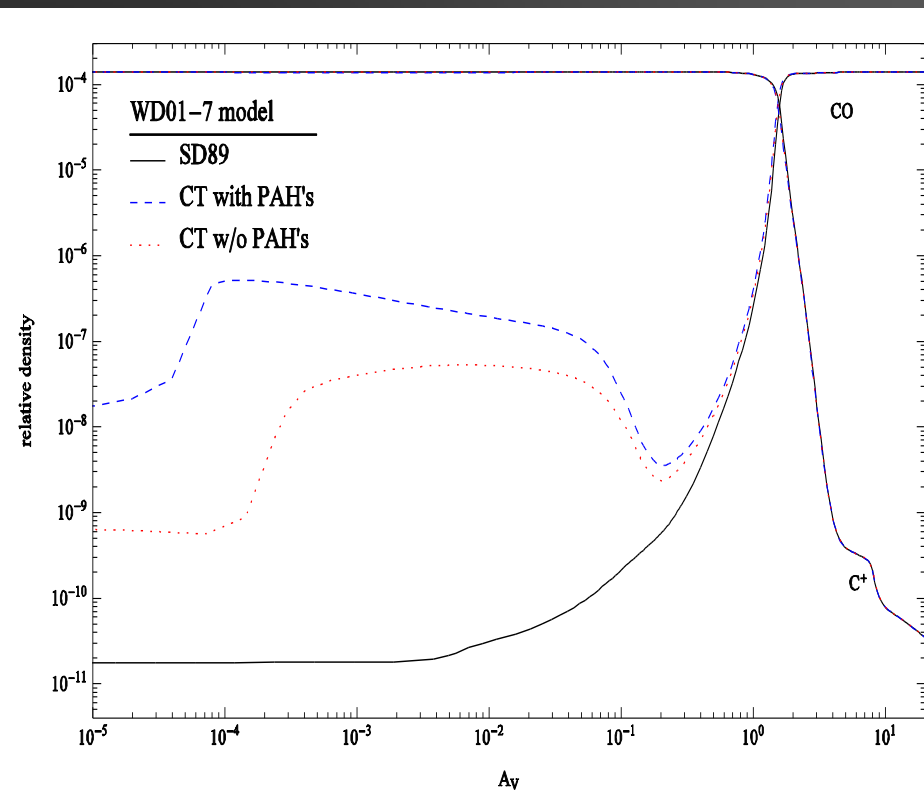


Dust influence

radiative transfer effect

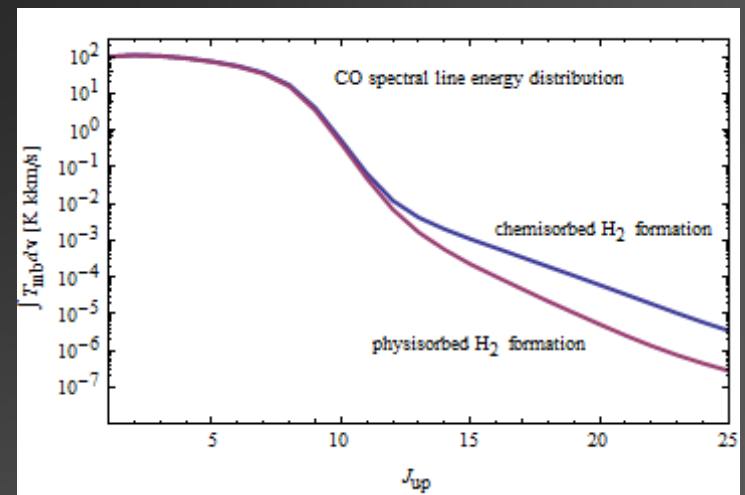
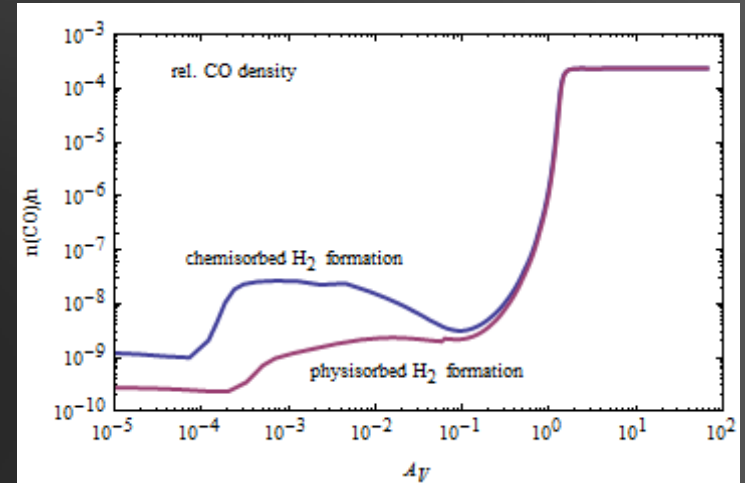


H₂ chemistry effect



Dust influence

- H_2 binding energy 4.5 eV
→ H_2 formation heating
- kinetic H_2 dissociation cooling
(Lepp & Shull, 1983, ApJ 270, 578)
 $\text{H}_2 + \text{H} \rightarrow \text{H} + \text{H} + \text{H} - 4.5\text{eV}$
 $\text{H}_2 + \text{H}_2 \rightarrow \text{H}_2 + \text{H} + \text{H} - 4.5\text{eV}$
- large effect on $\text{H}-\text{H}_2$ transition region chemistry

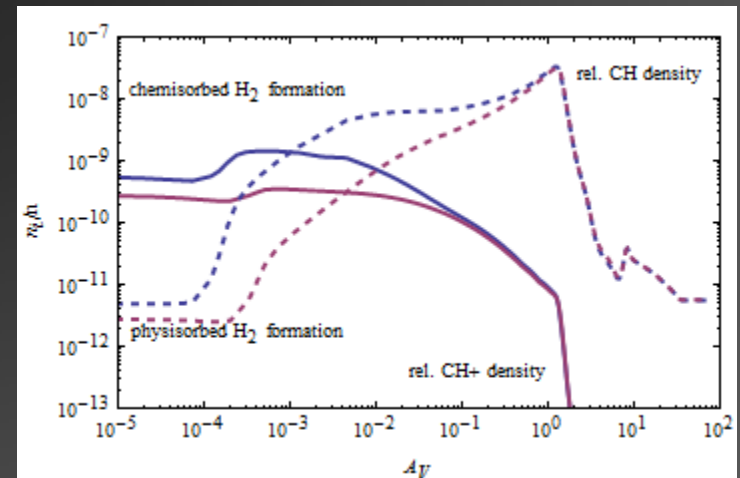
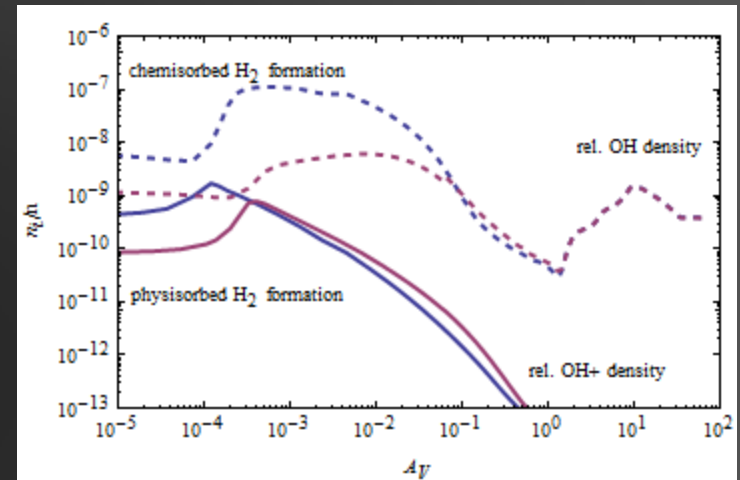


Dust influence

- H_2 binding energy 4.5 eV
→ H_2 formation heating
- kinetic H_2 dissociation cooling
(Lepp & Shull, 1983, ApJ 270, 578)



- large effect on H- H_2 transition region chemistry
- **chemistry ↔ physics**



Summary

- Great need for reliable (astrochemistry) data
- Lab results need to be robust against different modeling applications
- Growing understanding of dust properties and H₂ formation process dramatically influences model results
- chemistry and physics strongly connected to each other